LumiGauss: Relightable Gaussian Splatting in the Wild

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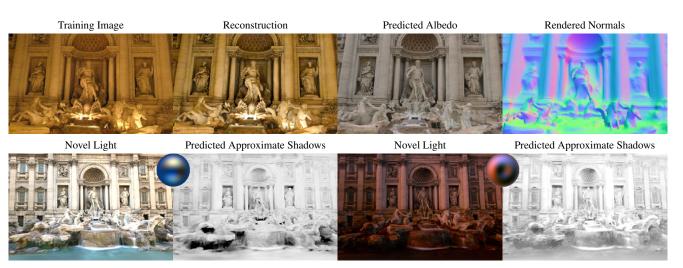


Figure 1. **Teaser** – LumiGauss reconstructs environment maps and object surfaces from *in-the-wild* images. Our model decouples the scene color and its normals (*second and fourth column in the top row*). At inference, it can synthesize novel views (*bottom row*) and realistic lighting (*first and third columns in the bottom*) with high-fidelity shadows (*second and fourth columns in the bottom*).

Abstract

Decoupling lighting from geometry using unconstrained photo collections is notoriously challenging. Solving it would benefit many users as creating complex 3D assets takes days of manual labor. Many previous works have attempted to address this issue, often at the expense of output fidelity, which questions the practicality of such methods. We introduce LumiGauss - a technique that tackles 3D reconstruction of scenes and environmental lighting through 2D Gaussian Splatting. Our approach yields high-quality scene reconstructions and enables realistic lighting synthesis under novel environment maps. We also propose a method for enhancing the quality of shadows, common in outdoor scenes, by exploiting spherical harmonics properties. Our approach facilitates seamless integration with game engines and enables the use of fast precomputed radiance transfer. We validate our method on the NeRF-OSR dataset, demonstrating superior performance over baseline methods. Moreover, LumiGauss can synthesize realistic images for unseen environment maps. Our code: https: //github.com/joaxkal/lumigauss.

1. Introduction

The colors emitted by objects are a combination of a spectrum of the light hitting the object and the material properties of that object. The light hitting the object's surface is a sum of the light scattered in the medium and bounced from neighboring objects [35]. In computer graphics, we often simplify this effect and decouple it into two entities: an intrinsic object's color or *albedo* and an omnidirectional texture representing the illumination [22]—*environment map.* Acquiring those assets enables the designing of realistic scenes in games or movies.

In many scenarios, creating realistic albedo textures and environment maps requires skilled technicians and artists to be involved in the process. To democratize it, the previous approaches [7, 23, 34] tried to use photographs taken with commodity cameras and *invert* the capturing process to recover albedo and an environment map. Given the abundance of casual, in-the-wild photographs available on the Internet, solving that issue is of high importance.

Recent advancements in reconstruction in-the-wild include NeRF-in-the-Wild [18] (NeRF-W). NeRF-W leverages neural radiance fields [19] which reconstruct a scene given its photos with calibrated cameras. NeRF-W can further work in realistic scenarios where the pictures come

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from the *in-the-wild* collections—the images in such may differ in the lighting conditions or scene content. However, NeRF-W and its follow-up works, HA-NeRF [3] and CR-NeRF [39], cannot decouple the object's albedo and the environment map, making it difficult to use in practice. NeRF-OSR [23] approaches that problem, but its shading model requires neural network execution at runtime, making integration with graphics engines difficult, and the reconstruction quality leaves space for improvement.

3D Gaussian Splatting [13] (3DGS) solves one of the main bottlenecks of NeRF - the training speed and output fidelity. In contrast to NeRFs, 3DGS models the scene as a composition of 3D Gaussians attributed with colors and opacity which are rasterized, or *splatted*, to render the output image. Recovering an object's surface from them requires specialized training techniques [9]. On the other hand, 2DGS [12] proposes reformulating 3D Gaussians as their 2D alternative where one of the axes is collapsed. The final scene representation ends up being composed of 2D *surfels* which provide a flat surface crucial for our relighting approach.

In this work, we propose LumiGauss, a method that uses 2DGS [12] to perform inverse graphics on images taken in the wild. In contrast to past approaches, our method is imbued with fast training and inference speed while maintaining high-quality renderings and being easy to integrate with graphics engines. In our method, the light is modeled as a combination of an environment map and a radiance transfer function that represents which parts of the environment map illuminate a given surfel-both are modeled by spherical harmonics [22]. This approach allows for modeling shadows, which is our main goal, but also has the potential to represent light reflected off of other objects. The output from LumiGauss enables both novel view synthesis and relighting using environment maps beyond those available during training. Leveraging the possibilities offered by the precomputed radiance transfer, our representation integrates seamlessly into game engines, enabling fast and efficient relighting.

Our contributions:

- We repurpose 2D Gaussian Splatting for an inverse graphics pipeline in an in-the-wild setting. With our approach, we recover high-quality albedo and environment maps.
- To enable shadows we learn the radiance transfer function for each 2D splat and represent it using spherical harmonics.
- Finally, we demonstrate that our reconstructed environment maps can be effectively used to relight arbitrary objects within graphic engines.

2. Related Works

Relighting. Relighting outdoor scenes is a key challenge in computer graphics and VR/AR. Early works [1, 5, 10, 14, 30, 31, 36] used training-free methods like statistical inference. Deep learning approaches, such as Yu <u>et al.</u> [40] with a neural renderer, and Philip <u>et al.</u> [20] with proxy geometry, face limitations in reconstruction quality and viewpoint flexibility.

NeRF-based methods [19] enabled simultaneous viewpoint and lighting changes. However, methods like [27,41, 44] handle a single illumination only or specific illumination setup during. Others are object-specific, such as for faces [29]. Many unconstrained photo collection methods focus on appearance, not lighting, complicating integration with other graphical components [3, 15, 18, 39].

NeRF-based approaches, such as [21] and [11], focus on inverse rendering for outdoor scenes, particularly in applications like autonomous driving. However, these methods are designed for single video sequences rather than unstructured photo collections. Rudnev et al. [23] proposed a method for relighting landmarks from unconstrained photo collections, using NeRF with external lighting extraction. Similarly, [16] compresses the per-image illumination into a disentangled latent vector. Wang et al. [34] target static scenes and works with unconstrained photo collections but rely on costly mesh extraction. Some methods incorporate additional priors, environmental assumptions, or regularizations [28, 38]. Gardner et al. [7] leverage externally trained models to provide environmental lighting priors. Despite their potential, these methods cannot be used in real-time applications due to NeRF's slow training and rendering times.

In contrast, the TensoRF-based approach by Chang <u>et</u> <u>al.</u> [2] aligns time information and sun direction with images for relighting, eliminating the need for external lighting models. While this method is faster than NeRF, it still lacks seamless integration with graphics engines and is unsuitable for synthetic light integration.

Notable Gaussian Splatting works designed for unconstrained photo collections [4, 13, 32, 37, 42] focused on appearance editing, not seamless graphical component integration. Relightable Gaussian approaches, like [6, 17, 25], tackle material decomposition but are not adapted to handle varying lighting conditions of *in-the-wild* training setup. Radiance transfer properties, employed in a similar way to LumiGauss, are utilized in [24, 43]. However, these methods rely on a burdensome dataset setup, restricting their applicability to specific use cases.

Gaussian Splatting. Kerbl <u>et al.</u> [13] introduced a notion of using learnable 3D Gaussian primitives from point clouds. Those Gaussians are parametrized with 3D covariance ma-

trix Σ_k and their location \mathbf{t}_k :

$$\mathcal{G}(\mathbf{t}) = \exp(\frac{1}{2}(\mathbf{t} - \mathbf{t}_k)^{\top} \Sigma_k^{-1}(\mathbf{t} - \mathbf{t}_k)), \qquad (1)$$

where the covariance matrix is factorized into a scaling diagonal matrix \mathbf{s}_k and a rotation matrix \mathbf{R}_k as $\Sigma_k = \mathbf{R}_k \mathbf{s}_k \mathbf{s}_k^\top \mathbf{R}_k^\top$. An image is rendered with a splatting operator $S(\cdot)$ which projects Gaussians into the camera coordinates with a world-to-camera matrix and then to image plane with a local affine transformation [45]:

$$\mathcal{S}(\mathcal{C}_c \mid \mathcal{G}) = \sum_{k=1}^{K} \mathbf{c}_k o_k \mathcal{G}_k \prod_{j=1}^{k-1} (1 - o_j \mathcal{G}_k).$$
(2)

The operator produces an RGB image, given a calibrated camera matrix C_c and their additional Gaussians' attributes: their colors c and opacities o. Attributes are learned using a stochastic gradient descent.

Huan et al. [12] argues that 3DGS although producing high-quality images, the implicit surface representation is noisy, limiting its applicability in relighting scenarios. They propose using 2D Gaussians instead to create smooth, coherent meshes thanks to their exact 2D surfel projection. We leverage that representation in our LumiGauss—a relightable model that decouples albedo, environment light and shadows thanks to our proposed physical constraints.

3. Method

3.1. Preliminaries on Radiance Transfer

The rendering equation, in its simplified form [8], is an integral function that represents light $L(\mathbf{x}, \boldsymbol{\omega}_o)$ exiting point \mathbf{x} along the vector $\boldsymbol{\omega}_o$:

$$L(\mathbf{x}, \boldsymbol{\omega}_o) = \int_s f_r(x, \boldsymbol{\omega}_o, \boldsymbol{\omega}_i) L_i(\mathbf{x}, \boldsymbol{\omega}_i) D(\mathbf{x}, \boldsymbol{\omega}_i) d\boldsymbol{\omega}_i \quad (3)$$

where $f_r(\cdot)$ is a BRDF function, $L_i(\cdot)$ an incoming light along the vector ω_i , and $D(\cdot)$ is a radiance transfer function. Intuitively, $f_r(\cdot)$ represents the surface material, $L_i(\cdot)$ represents the intensity and color of the illumination, and $D(\cdot)$ is a term that takes into account shadows or light reflections from other surfaces. Depending on the formulation of those functions, the rendering equation can range from a straightforward and inaccurate light model to a highly complex and accurate one.

Unshadowed model. One example of a reflection model that can be represented with Eq. (3) is the diffuse surface reflection model, also known as *dot product lighting*. A diffuse BRDF reflects light uniformly, making the lighting view-independent and simplifying the BRDF as follows:

$$L_D(\mathbf{x}) = \frac{\rho(\mathbf{x})}{\pi} \int_s L_i(\mathbf{x}, \boldsymbol{\omega}_i) \max(\mathbf{n}(\mathbf{x}) \cdot \boldsymbol{\omega}_i, 0) d\boldsymbol{\omega}_i \quad (4)$$

where $\rho(\cdot)$ is the surface albedo, $\mathbf{n}(\mathbf{x})$ a surface normal at the point x. Shadows are neglected.

The incoming light $L_i(\mathbf{x}, \boldsymbol{\omega}_i)$ can be represented in several ways. In this work, we assume that the scene is illuminated with an **omnidirectional environment map** that is parametrized using spherical harmonics (SH) of degree nwith $(n+1)^2$ coefficients. Because the environment map is positioned infinitely far from the scene, the light is positionindependent, and thus, the rendering equation is further simplified:

$$L_U(\mathbf{x}) = \frac{\rho(\mathbf{x})}{\pi} \int_s L_i(\boldsymbol{\omega}_i) \max(\mathbf{n}(\mathbf{x}) \cdot \boldsymbol{\omega}_i, 0) d\boldsymbol{\omega}_i \quad (5)$$

With illumination parametrized with SH, we can evaluate the integral in Eq. (5) using a closed-form solution from Eq. (12) in [22]. From this point onward, we refer to rendering with Eq. (5) as *unshadowed*.

Shadowed model. In addition to the *unshadowed* lighting model, we propose a *shadowed* model, where $D(\mathbf{x}, \omega_i)$ is parameterized using spherical harmonics (SH) and learned from training data. In $D(\mathbf{x}, \omega_i)$, SH represents a spherical signal that quantifies the light arriving from each direction of the environment map to an associated point in space. The *shadowed* model is derived by replacing the dot product term in Eq. (5):

$$L_S(\mathbf{x}) = \frac{\rho(\mathbf{x})}{\pi} \int_s L_i(\boldsymbol{\omega}_i) D(\mathbf{x}, \boldsymbol{\omega}_i) d\boldsymbol{\omega}_i.$$
 (6)

In addition to modeling shadows, this approach also has the potential to model the interreflection of light between objects in the scene.

Using SH of the same degree for both the environment map and transfer function allows efficient evaluation of the rendering equation Eq. (6). A key SH property simplifies the integral of two SH-based functions to a dot product of their coefficients, thanks to SH orthogonality. With this property Eq. (6) can be re-written as:

$$L_S(\mathbf{x}) = \frac{\rho(\mathbf{x})}{\pi} \mathbf{l} \cdot \mathbf{d},\tag{7}$$

where $\mathbf{l} \in R^{(n+1)^2}$ are the SH coefficients of $L_i(\boldsymbol{\omega}_i)$ and $\mathbf{d} \in R^{(n+1)^2}$ are the SH coefficients of $D(\mathbf{x}, \boldsymbol{\omega}_i)$. Please see [8, 26] for derivation. This property is commonly used in real-time rendering where the radiance transfer function is pre-computed and only Eq. (7) is evaluated at runtime.

3.2. LumiGauss

LumiGauss creates a 3D representation of a relightable model using 2D Gaussians [12] from $c \leq C$ images taken *in-the-wild* $\{\mathcal{I}_c\}_{c=1}^C$ with associated calibrated cameras $\{\mathcal{C}_c\}_{c=1}^C$. Our goal is to find Gaussian parameters $\mathcal{G} = \{\mathbf{t}_k, \mathbf{R}_k, \mathbf{s}_k, o_k, \boldsymbol{\rho}_k, \mathbf{d}_k\}_{k=1}^K$ that after the rasterization [13] recreate those images. We optimize Gaussians by

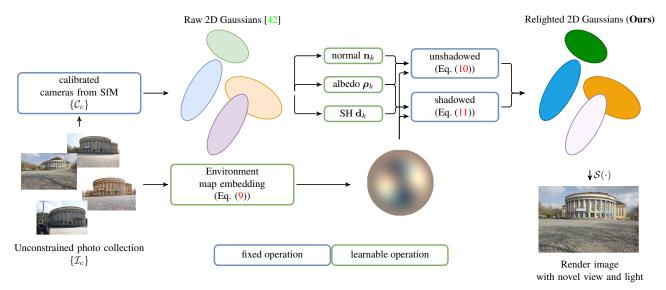


Figure 2. **Pipeline** – LumiGauss learns the relightable 2D Gaussian [42] representation from unconstrained photo collection with variable camera parameters and lighting conditions. Each of k Gaussians holds: a normal n_k , albedo ρ_k , and learnable transfer function d_k . Our contributed method composes the Gaussians in two modes—*shadowed* and *unshadowed*. The *shadowed* model reconstructs additional shadows (see Fig. 1) on top of the unshadowed model thanks to our proposed use of a radiance transfer function. The Gaussians are splatted [13, 42] to render the output image in a novel view and light.

minimizing the objective:

$$\underset{\mathcal{G},\mathcal{E},\boldsymbol{\theta}}{\arg\min} \mathbb{E}_{\mathcal{C}_{c} \sim \{\mathcal{C}_{c}\}} \underbrace{\ell_{\text{rgb}}(\mathcal{S}(\mathcal{C}_{c} \mid \mathcal{G}, \mathcal{E}, \boldsymbol{\theta}), \mathcal{I}_{c})}_{\text{Sec. 3.4}} + \underbrace{\mathcal{R}(\mathcal{G})}_{\text{Sec. 3.3}}, \quad (8)$$

where $\mathcal{E} = \{\mathbf{e}_c\}_{c=1}^C$ is a set of scene-dependent, learnable environment embeddings, ℓ_{rgb} is a photometric objective that compares the rendered image from an operator $\mathcal{S}(\cdot)$ (Eq. (2)), and \mathcal{R} are additional regularization terms. In contrast to 2DGS [12], for each Gaussian we model the base color ρ as diffuse¹, and introduce SH coefficients for the transfer function d². 2DGS provides smooth normals that make relighting possible.

In what follows, we drop the dependence of functional forms on the positions x we introduced in Sec. 3.1 for brevity.

Relighting. To handle the diverse lighting conditions in *in-the-wild* images, we associate each training image with a learnable latent code e_c that encodes its lighting conditions. Using this embedding, we predict the environment map coefficients via an MLP:

$$\mathbf{l}_c = \mathrm{MLP}(\mathbf{e}_c | \boldsymbol{\theta}), \tag{9}$$

where $\mathbf{l}_c \in \mathbb{R}^{3 \times (n+1)^2}$ represents the SH coefficients of the environment map, and n=2 is the SH degree. As shown in [22], second-order SH is sufficient to approximate environment lighting in many scenarios.

The predicted illumination is used in the rendering process in one of two ways: *unshadowed* and *shadowed*. Those two approaches correspond to Eq. (5) and Eq. (7) respectively, and are described below.

Unshadowed model. For the unshadowed scenario, we follow Eq. (5), which integrates light over the hemisphere in the direction of the surface normal. The color \mathbf{c}_k , *radiance*, for each Gaussian \mathcal{G}_k given its normal \mathbf{n}_k and the illumination parameters \mathbf{l}_c equates to:

$$\mathbf{c}_{k} = \boldsymbol{\rho}_{k} \odot \underbrace{\mathbf{n}_{k}^{t} M(\mathbf{l}_{k}) \mathbf{n}_{k}}_{\text{unshadowed irradiance}}, \quad (10)$$

where M is a 4×4 matrix derived from the SH parameters of the environment map. It is the closed form solution of the integral in Eq. (5), please see Eq. (12) in [22] for details.

This simple yet effective model already imbues the model with relighting capabilities. However, as described in Fig. 3 it does not capture shadows correctly, limiting the output's fidelity.

Shadowed model. To effectively capture shadows in the model, we redefine the output color of a Gaussian as \tilde{c}_k , a function of learnable radiance transfer function D_k parametrized by spherical harmonics $\mathbf{d}_k \in \mathbb{R}^{(n+1)^2}$, light \mathbf{l}_c and albedo $\boldsymbol{\rho}_k$. Using a learned radiance transfer function (instead of fixing it to capture light from the hemisphere above the normal as we do in *unshadowed*) allows for creating shadows, as described in Sec. 3.1. Overall, following

¹As per Sec. 3.1, view-dependent effects are not modeled in diffuse reflections.

²These coefficients correspond to a single channel in practice.

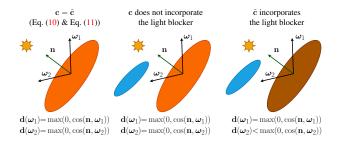


Figure 3. Unshadowed \mathbf{c} (Eq. (10)) and shadowed $\tilde{\mathbf{c}}$ (Eq. (11)) may give the same output color if a Gaussian is fully exposed to the environment light. In the case of any occluder, \mathbf{c} does not handle, and the color does not change. However, our proposed $\tilde{\mathbf{c}}$ properly reacts to the occluder and makes the output color darker.

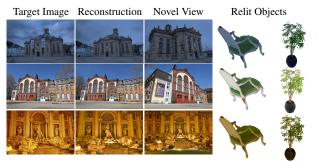


Figure 4. Scene reconstruction and relightning – Reconstruction and relighting capabilities of LumiGauss. LumiGauss reproduces sharp and clean landmarks, and the learned environment lighting enables accurate scene relighting. We use learned environment maps to relight the scene from novel viewpoints and then relight arbitrary objects within a graphics engine.

Eq. (7), the output shadowed color or *radiance* reduces to:

$$\tilde{\mathbf{c}}_{k} = \boldsymbol{\rho}_{k} \odot \underbrace{\sum_{i=1}^{(n+1)^{2}} \mathbf{l}_{c}^{i} \cdot \mathbf{d}_{k}^{i}}_{\text{shadowed irradiance}}, \quad (11)$$

As we show later in the experiments, the addition of shadows leads to more accurate relighting. Additionally, it does not require learnable MLP to reconstruct shadows at the inference stage, differentiating it from NeRF-OSR [23] and making our approach applicable to rendering engines directly.

3.3. Physical constraints

The regularizations proposed in 2DGS [12] keep the Gaussians close to the surface and smooth locally, which is crucial in our relighting scenario. Aside from them, we propose new loss terms based on the physical light properties that restrict the optimization from achieving degenerate, *non-relightable* cases. We restrict radiance transfer D_k function to remain within the range of 0 to 1, where 0 indicates complete shadowing and 1 signifies full expo-

sure to lighting:

$$\ell_{0-1} = \mathbb{E}_k \mathbb{E}_{\boldsymbol{\omega}_i} [\| \max(D_k(\boldsymbol{\omega}_i), 1) - 1 \|_2^2 \\ + \| \min(D_k(\boldsymbol{\omega}_i), 0) \|_2^2],$$
(12)

and allow the environment light to remain in the \mathbb{R}_+ domain:

$$\ell_{+} = \mathbb{E}_{k} \mathbb{E}_{\boldsymbol{\omega}_{i}} \| \min(L_{c}(\boldsymbol{\omega}_{i}), 0) \|_{2}^{2},$$
(13)

which allows the environment light to brighten the scene arbitrarily.

The shadowed radiance transfer should remain close to the unshadowed version. If not, the shadowed version might include light from any direction, resulting in degenerate solutions and incorrect relighting. We visualize the shadowed and unshadowed transfer functions in Fig. 3. To address this issue, we propose the following loss function:

$$\ell_{\mathbf{0}\leftrightarrow\mathbf{0}} = \mathbb{E}_k \mathbb{E}_{\boldsymbol{\omega}_i} \| \max(\mathbf{n}_k \cdot \boldsymbol{\omega}_i, 0) - D_k(\boldsymbol{\omega}_i) \|_2^2, \quad (14)$$

The applied transfer function inherently accounts for shadows and interreflections. To focus specifically on modeling shadows and restrict the use of Eq. (11) for other cases, we impose a loss function ensuring that shadowed radiance should not be brighter than unshadowed one:

$$\ell_{\mathbf{0}} = \mathbb{E}_k \mathbb{E}_{\boldsymbol{\omega}_i} \| \max(D_k(\boldsymbol{\omega}_i) - \max(\mathbf{n}_k \cdot \boldsymbol{\omega}_i, 0), 0) \|_2^2,$$
(15)

Those losses are weighted with scalars $\{\lambda_{1,...,4}\}$ fixed across experiments and contribute to our regularization term:

$$\mathcal{R}(\mathcal{G}) = \lambda_1 \ell_{0-1} + \lambda_2 \ell_+ + \lambda_3 \ell_{\bullet \leftrightarrow \bullet} + \lambda_4 \ell_{\bullet}$$
(16)

Calculating it exactly requires us to compute the expectation over the hemisphere \mathbb{S}^2 . Instead, we approximate the expectations over directions ω_i with a Monte Carlo estimator by randomly sampling the SH lobe with N samples at each training step.

3.4. Reconstruction

We render images using the splatting algorithm $S(\cdot)$ proposed in 2DGS [12]. We compare the rendered images with ground-truth $\{\mathcal{I}_c\}$ taken with $\{\mathcal{C}_c\}$ cameras. Our method builds on 2DGS [12] and therefore our reconstruction loss ℓ_{rgb} follows the following term:

$$\ell_{\rm rgb} = \lambda_{\rm rec}(\mathbf{0})\ell_{\rm rec}(\mathbf{0}) + \lambda_{\rm rec}(\mathbf{0})\ell_{\rm rec}(\mathbf{0}), \qquad (17)$$

$$\ell_{\text{rec}}(\{\mathbf{0},\mathbf{0}\}) = \ell_1(\{\mathbf{0},\mathbf{0}\}) + \lambda \ell_{\text{D-SSIM}}(\{\mathbf{0},\mathbf{0}\}), \quad (18)$$

where the ℓ_1 is the L_1 loss comparing either the image rendered from our shadowed or unshadowed models and $\ell_{\text{D-SSIM}}$ is a differentiable D-SSIM [33] further improving the quality. We use λ =0.2 throughout all the experiments. Our proposed $\ell_{\text{rec}}(\circ)$ resembles a pretraining stage.

Table 1. **Quantitative results** – Comparison between our LumiGauss and selected baselines for two different . We report the reconstruction quality regarding PSNR, MSE, MAE, SSIM on full and 4x downsampled image resolutions. *u/s* denotes using upsampled, *d/s* downsampled images for the evaluation, and the last delimited area presents the ablation study on downsampled data. We denote NeRF-OSR [23] results reproduced by FEGR [34] with *. We use † to further annotate our approach where we remove loss terms $\ell_{\bullet\leftrightarrow\circ}$, $\ell_{rec}(\circ)$ from the second training stage. In ‡, we omit the first training stage. Compared to the baselines, LumiGauss achieves reconstructions of high fidelity. It reliably produces smooth surfaces and sharp edges, reflected in its high SSIM values. Additionally, our proposed components either enhance reconstruction or preserve physical accuracy without negatively impacting the results. Please note, that NeuSky [7] is a concurrent work, published prior to the WACV's deadline at ECCV 2024.

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Method	$\overline{\text{PSNR}}$ \uparrow	$MSE\downarrow$	$\text{MAE}\downarrow$	SSIM \uparrow	$\overline{\text{PSNR}\uparrow}$	$\text{MSE}\downarrow$	$MAE \downarrow$	$\text{SSIM} \uparrow$	PSNR ↑	$MSE\downarrow$	$\text{MAE} \downarrow$	$\mathbf{SSIM} \uparrow$
Yu et al. $_{u/s}$ [40]	15.17	0.033	0.133	0.376	17.87	0.017	0.097	0.378	15.28	0.032	0.138	0.385
Philip et al. [20]	12.28	0.062	0.179	0.319	16.63	0.023	0.113	0.367	12.34	0.065	0.200	0.272
NeRF-OSR [23]	16.65	0.024	0.114	0.501	18.72	0.014	0.090	0.468	15.43	0.029	0.133	0.517
NeRF-OSR* [23]	15.66	0.029	-	-	19.34	0.012	-	-	16.35	0.027	-	-
SR-TensoRF [2]	16.74	0.024	0.093	0.653	17.30	0.021	0.096	0.542	15.43	0.030	0.111	0.632
FEGR [34]	17.57	0.018	-	-	21.53	0.007	-	-	17.00	0.023	-	-
SOL-NeRF [28]	17.58	0.028	-	0.618	21.23	0.008	-	0.749	18.18	0.019	-	0.680
NeuSky [7]	18.31	0.016	-	-	22.50	0.005	-	-	16.66	0.023	-	-
Ours	18.01	0.017	0.096	0.778	19.59	0.012	0.085	0.700	17.02	0.021	0.107	0.729
Yu et al. [40]	15.84	0.028	0.123	0.392	18.71	0.014	0.088	0.400	15.43	0.031	0.136	0.363
Philip et al. d/s [20]	12.85	0.054	0.169	0.164	17.37	0.019	0.105	0.429	11.85	0.070	0.210	0.184
NeRF-OSR $_{d/s}$ [23]	17.38	0.021	0.106	0.576	19.86	0.011	0.080	0.626	15.83	0.026	0.128	0.556
Ours _{d/s}	18.40	0.016	0.094	0.746	20.13	0.011	0.080	0.727	17.24	0.020	0.105	0.715
Ours †	15.03	0.034	0.139	0.58	19.34	0.015	0.094	0.693	16.09	0.028	0.124	0.665
Ours ‡	17.59	0.019	0.100	0.733	19.05	0.016	0.097	0.680	16.83	0.022	0.110	0.694
Ours $\setminus \ell_{0-1}$	18.30	0.016	0.095	0.744	20.15	0.010	0.080	0.734	17.25	0.020	0.105	0.712
Ours $\setminus \ell_+$	17.35	0.020	0.104	0.728	20.17	0.012	0.081	0.729	17.10	0.020	0.106	0.703

Table 2. **Performance comparison –** Training time and inference speed comparison between the baselines and our LumiGauss.

Method	Training time	FPS		
NeRF-OSR [23]	31h	0.003		
NeuSky [7]	14h	0.004		
Ours	1h 20min	20.7		

As the more complex shadowed model lands in local minima if trained from scratch, we initiate the training with $\lambda_{rec}(\mathbf{0})=0.0$ and $\lambda_{rec}(\mathbf{0})=1.0$. Once the simpler model converges, we switch $\lambda_{rec}(\mathbf{0})=1.0$ and $\lambda_{rec}(\mathbf{0})$ to a small value so as not to deteriorate the quality of the model. In short, the shadowed model explains the parts of an image with shadows, which the unshadowed could not with its simpler lighting model.

4. Experiments

4.1. Datasets and baselines

To evaluate our approach, we followed the protocol from NeRF-OSR [23] using ground truth environment maps. We use the official data split for Staatstheatert, Landwehrplatz, and Ludwigskirche. We use segmentation masks for test images provided in the OSR dataset and calculate MSE, MAE, SSIM and PSNR on masked regions only. We compare LumiGauss against several NeRF-based baselines³ and TensoRF baseline. We provide the implementation details in Supplementary.

4.2. Scene reconstruction and relightning

We present the qualitative results in Tab. 1 and quantitative in Figs. 4 and 5. As Yu <u>et al.</u> [40] evaluates their model on downsampled images, we show the metric values on downsampled (d/s), and upsampled (u/s) to identify the quality differences. As we can see, LumiGauss performs better or on par with the baselines. NeuSky [7] is a concurrent work which models the environment maps and the sky using a prior, pretrained model.

As our backbone, 2DGS [12] incorportates priors to produce sharp edges and smooth surfaces, our model inherently performs better as expressed by SSIM. Please also see the zoom-ins in Fig. 5. Those shape reconstruction qualities allow us to relight the scene with high fidelity. We demonstrate that in Fig. 7 where one can see that our method effectively relights landmarks under various lighting conditions. We finally visualize the rendered shadows produced thanks to our proposed physical constraints at training time. Since

³We include the concurrent NeuSky [7] which has been published officially after the WACV deadline.

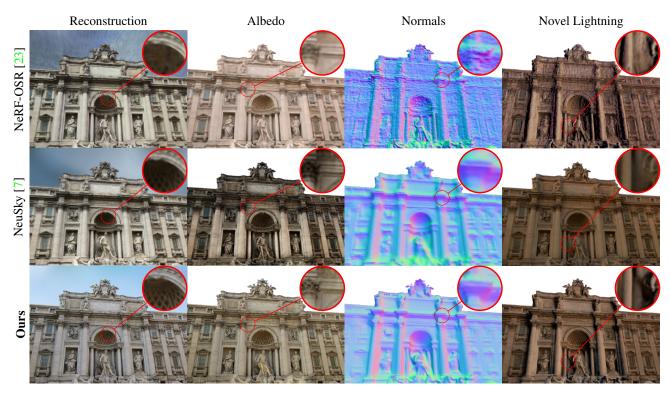


Figure 5. Qualitative comparison of albedo, normals, and relighting under similar lighting conditions on Trevi Fountain. LumiGauss produces albedo with fewer baked-in shadows, sharp normals, smooth surfaces, and more accurate novel lighting compared to the baselines. Results for NeuSky originally reported in [7]. Please, zoom in for details.

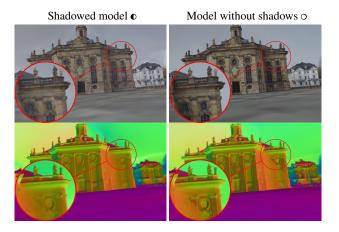


Figure 6. Effects of shadowed training – We show the comparison of **albedo** between the shadowed (*left*) and unshadowed (*right*) models. The albedo in the shadowed training is brighter with fewer shadows. The shadowed model recovers more accurate normals.

LumiGauss does not predict shadows explicitly, we visualize them as grayscaled difference of output irradiances between the *unshadowed* (Eq. (10)) and *shadowed* (Eq. (11)) to approximate shadow effects:

$$\max(\mathfrak{g}(\mathbf{c}_k \oslash \boldsymbol{\rho}_k - \tilde{\mathbf{c}}_k \oslash \boldsymbol{\rho}_k), 0), \qquad (19)$$

where \oslash is an element-wise division and $\mathfrak{g}(\cdot)$ converts from the RGB space to the grayscale space.

We also display the illumination in Fig. 7 to differentiate between shadows and dark illumination from the environment map. Additional detailed results on scene reconstruction, relightning and more comparisons to other works are included in Supplementary.

4.3. Ablations

We prioritize enhancing relighting capabilities over accurate appearance recreation during the optimization process, contrasting with recent Gaussian splatting methods that target novel view synthesis based on unconstrained photo collections [4, 37, 42]. Consequently, our ablation study primarily focuses on the degradation of relighting capabilities when removing any of the proposed components. We compare shadowed and unshadowed modeling and investigate the contributions of each loss term. We present the results in Tab. 1.

Gaussians can optimize to shadowed surfaces and represent shadows as normals and albedo colors (effect known as albedo/illumination ambiguity). Therefore, gains from separating shadows from lightning are not visible in metrics computed on a limited data subset. We noticed that adding a shadowed version can help restore proper albedo



Figure 7. Environment map rotation – The top row shows the illumination entering the scene. The second and third rows display the shadowed and unshadowed renderings, respectively. The last row represents the approximate predicted shadows. Please zoom in for details.

and normal vectors of surfaces that during the training were distorted or had low brightness (see Fig. 6).

4.4. Performance comparison

We compare LumiGauss' efficiency with two NeRF baselines. Our method achieves plausible relightning results while being orders of magnitudes faster both in terms of training and inference as shown in Tab. 2.

4.5. Limitations

We identify the following limitations of our approach. Notably, surface albedo and normals may attempt to simulate shadows in scenarios with hard and frequent shadows. This can pose challenges for shadow training, especially when shadows are visible in several training images, potentially hindering the accurate representation of surface normals. Incorporating priors for environment light and shadowing could further enhance disentanglement and light transport modeling as presented in the concurrent NeuSky [7]. While we assume diffuse albedo, valid for most outdoor cases, shadows can appear unnaturally on reflective surfaces such as windows. Separate background optimization could enhance the synthesis of scenes with extensive sky areas. Finally, our shadow modeling baked-in the spherical harmonics representations is non trivial to extend to dynamic applications, such as autonomous driving.

5. Conclusions

We present LumiGauss—the method capable of decoupling environment lighting and albedo of objects from images *in-the-wild*. To this end, we apply 2DGS [12] to reconstruct the object's surface accurately and then use our proposed training components that correctly disentangle light properties from the rendered colors. As we show in the experiments, our approach achieves better reconstruction results than the baselines. We also present that one of our contributions—modeling shadows via leveraging Spherical Harmonics properties—provides shadows of high fidelity that react appropriately to changing environment light. LumiGauss is a novel approach in the direction of inverting the rendering process from images *in-the-wild*, reconstructing high-quality scene properties without sacrificing the fidelity of the output.

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A. Dataset Processing

Occluders. To exclude occluders from training images we use masks provided with OSR dataset [23].

Test set. We test our approach on 5 viewpoints for each scene, as it was originally proposed in [23]. For testing, we use test masks provided by [23] and we stricly follow their evaluation protocol. For SSIM, we report the average value over the segmentation mask, utilizing the scikit-image implementation with a window size of 5 and eroding the segmentation mask by the same window size to exclude the influence of pixels outside the mask on the metric value.

Testing with ground truth environment map. The authors of [7] made an effort to recover steps for environment map preprocessing and alignment. The preprocessing step is available in their repository, accessible at: https://github.com/JADGardner/neusky/blob/main/notebooks/nerfosr_envmaps.ipynb. The detailed discussion on SOL-NeRF [28] approach to environment map alignment is included in the NeuSky main paper [7] and also confirmed with SOL-NeRF authors.

B. Implementation details

The appearance embedding vector is set to a size of 24 dimensions. For predicting the environment map, we use MLP with 3 fully-connected layers of size 64. We trained all models for 40000 iterations, the first training stage is set to 20000 iterations. The learning rate for MLP and embedding is set to 0.002, which after first training stage is reduced to 0.0002. We train gaussian spherical harmonics with a learning rate of 0.002. We set the loss function weights as follows: for $\ell_{0-1} \lambda_1 = 0.001$, for $\ell_+ \lambda_2 = 0.05$, for $\ell_{0 \leftrightarrow 0} \lambda_3 \in \{1.0, 10.0\}$, for $\ell_0 \lambda_4 = 10.0$. In the second training stage we set $\lambda_0 = 0.001$.

We adhere to the original Gaussian splatting densification and pruning protocols, with a densification interval of 500 iterations and an opacity reset interval of 3000 iterations. We apply regularizations to align Gaussians with surfaces, as originally described in [12]. Additionally, we utilize the dual visibility concept proposed in [12]. This ensures that the Gaussians are always correctly oriented towards the camera. Dual visibility effectively produces consistent world normals, with visible normals being consistent and non-visible ones contributing minimally to the rendering. Regularization of Spherical Harmonics d_k is dependent on gaussian normals. Since normals are rotated to always face the camera, to maintain alignment between each Gaussian's normal and its associated d_k , we also rotate d_k accordingly.

We run all experiments using a single NVIDIA A100 80GB or RTX 2080 Ti 128 GB.

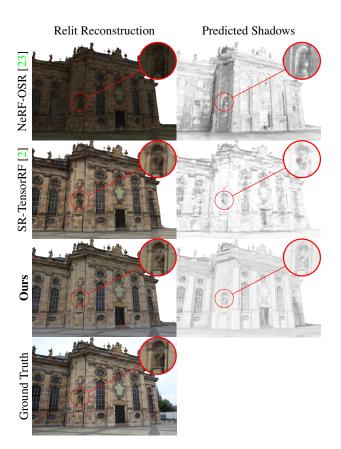


Figure 8. Qualitative comparison of scene reconstruction for the selected photo session. Results for NeRF-OSR [23] and LumiGauss were genrated using ground truth environment maps for selected photo session, while ST-TensoRF [2] used extracted timestamp. Results for NeRF-OSR and SR-TensorF reported originally in [2].

C. Relighting - additional results

Please reach for additional results to videos the attached (https://drive . drive / folders qooqle . com 1 1AvKkg0MMWPsftFXMPoeuV3jCkmox3XxN ? usp = sharing).

D. Qualitative comparison - additional results

In Fig. 8 we show the qualitative comparison of our method, NeRF-OSR, and SR-TensoRF. We show the land-mark relit with ground truth envoronment map for NeRF-OSR and LumiGauss. SR-TensoRF reconstructs ground truth using only daytime (timestamp).

In Fig. 10, we show the qualitative comparison of our method, NeRF-OSR, and SR-TensoRF. We use the *default synthetic* environment map provided by [23]. This environment map was used for visualisation purposes in [2]. We use it to ensure a fair comparison and consistency with results

from concurrent works. We also present albedo and normals extracted from the reconstructed scene. Please note that our model produces much cleaner results. Compared to the baselines, it reconstructs sharp features in small elements of the buildings, which is also reflected in the quantitative results Tab. 1. LumiGauss also gracefully smooths out the elements of scenes that are variable across the images, such as trees and clouds. On the other hand, NeRF-OSR and SR-TensoRF produce artifacts that negatively impact the output reconstructions.

In Fig. 9 we present additional comparison with concurrent works. We focus on normal and albedo quality.

In Fig. 11 we present additional results of novel view synthesis and comparison with concurrent works. Similarly to NeRF-OSR, we relight our scenes with the **default synthetic** map provided by NeRF-OSR for visualization purposes. This environment map does not correspond to GT images.

E. Ablation study - additional results

In Fig. 12 we present renders from training without selected regularization terms.

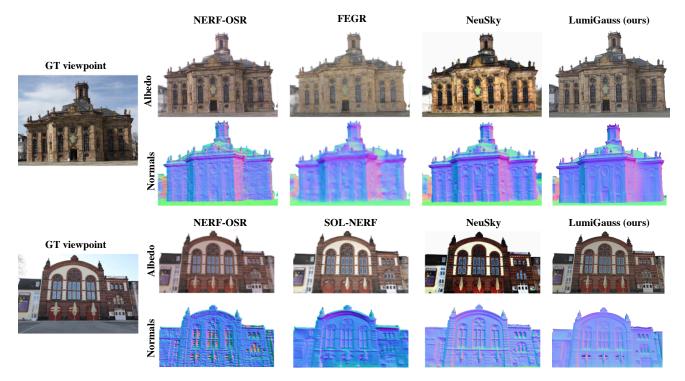


Figure 9. Qualitative comparison of predicted albedo and rendered normals. Results for NERF-OSR, FEGR, SOL-NERF, NeuSky reported originally in [7].

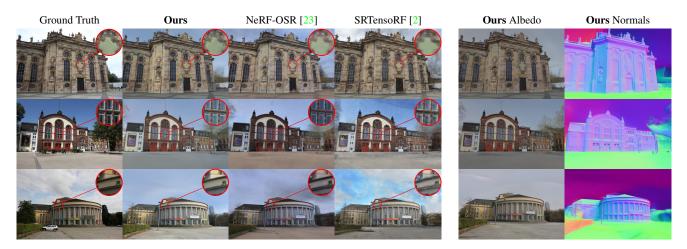


Figure 10. **Qualitative results –** Showcase of novel view synthesis using shadowed radiance transfer. We present albedo and normals produced by our method. Our method generates much sharper renderings. Please see zoom-ins to see details on the quality difference, such as surface smoothness and edge sharpness of small building elements. We use visual results for SR-TensoRF and NeRF-OSR presented originally in [2]. Please note that, in this comparison the environment map used to create renders for NeRF-OSR and LumiGauss **does not match** the illumination in ground truth. LumiGauss and NeRF-OSR employ the **default** environment map provided by NeRF-OSR **for clear visualisation purpose only**. SR-TensoRF do not rely on any environment map, instead it utilizes daytime information.

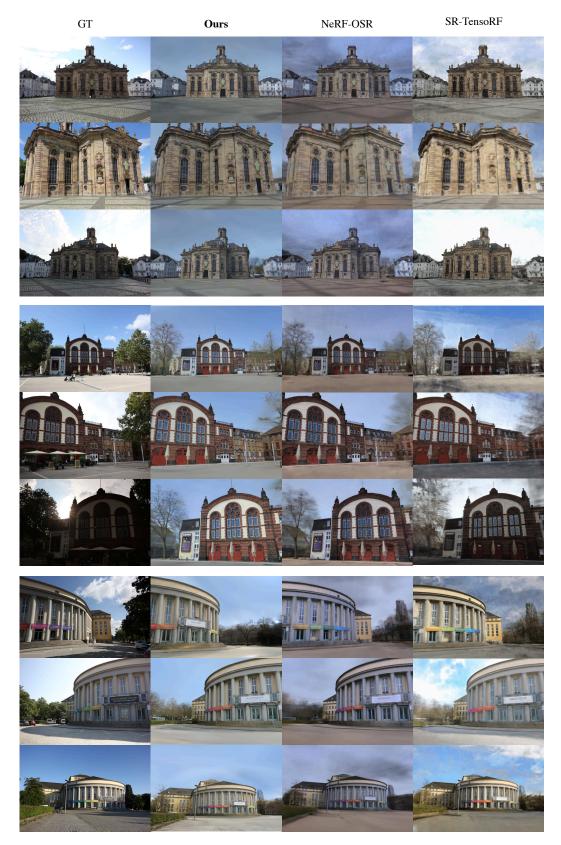


Figure 11. **Qualitative comparison.** Additional novel viewpoints. Results for NeRF-OSR and SR-TensoRF originally reported in [2]. Please note, in this comparison renders for NeRF-OSR and LumiGauss **do not have to** reconstruct ground truth. LumiGauss and NeRF-OSR employ the **default** environment map provided by NeRF-OSR **for clear visualisation purpose only**.



Figure 12. Ablation study for relightning with external environment map. The full model results in the clearest render. The strongest quality drop is observed when components restricting D_k are omitted.